

ROBUST AND EFFICIENT COMPRESSION OF LIST OF ITEMS

This application claims priority from U.S. Provisional Application No.

5 60/211,986, filed June 16, 2000, and entitled "Robust and Efficient Compression of
List of Items," the subject matter of which is incorporated herein by reference.

FIELD OF THE INVENTION

The present invention relates to compression of a list of items.

BACKGROUND OF RELATED ART

10 Internet Protocol (IP) is widely used in different types of networks. For
example, for IP based real-time multimedia, Real-Time Transfer Protocol (RTP) is
predominantly used on top of User Datagram Protocol (UDP) and IP version 4 (IPv4)
or IP version 6 (IPv6). However, due to the large size of IP/UDP/RTP header, which
is undesirable in low bandwidth networks such as wireless networks, suitable header
15 compression schemes are needed.

Header compression algorithms are based on the observation that most fields of
the IP packet headers remain constant in a packet stream during the length of a
session. Thus, it is possible to compress the header information by establishing a
context at both compressor and decompressor and by simply carrying a minimal
20 amount of header information from the compressor to the decompressor. Header
compression schemes need to be robust so that they can tolerate loss and residual

errors on the link over which header compression takes place without losing additional packets or introducing additional errors in the decompressed headers.

There are several types of item lists inside IP/UDP/RTP headers. Item lists include a list of items. Examples include, but are not limited to, Contributing Source (CSRC) list in RTP header, IPv6 Extension Header Chain, Address List in type 0 Routing Header. The Internet Engineering Task Force (IETF) Robust Header Compression (ROHC) Working Group recognizes the problem of how to compress an item list that may vary in composition from application to application. It is desirable to obtain a general and efficient solution applicable to different types of header fields or different applications.

SUMMARY OF THE INVENTION

To solve the above and other problems, embodiments of the present invention may provide a method of communicating information. The method may include comparing a current item list with a reference item list and determining a type of classification based on the comparison. A difference may be determined between the current item list and the reference item list and this difference may be sent from a first entity to a second entity. Information regarding the difference may be encoded prior to sending the information from the first entity to the second entity.

A compressed list may be sent from a first entity to a second entity. The compressed list may include information regarding the difference between the current item list and the reference item list. The difference may be encoded within the

compressed list based on the determined type of classification. The type of classification may be based on one of: whether an item in the reference item list is in the current item list, whether the item is in the reference item list and whether contents of the item in the current item list are the same as contents of the item in the reference item list.

5 In at least one embodiment, a difference may be determined between one item in the current item list and a corresponding item in the reference item list. This difference may be sent from one entity to the other entity.

10 The method may also include sending the reference item list from a first entity to a second entity. Information sent from the first entity to the second entity may be decompressed using the previously sent reference item list as a reference.

15 Embodiments of the present invention may also provide a device to communicate information that includes a processor device to classify at least one item of a list and to form a compressed list including the at least one item. A transmitting device may transmit the compressed list. Further, an encoding device may encode information for transmission by the transmitting device to another entity.

Other objects advantages and salient features of the invention will become apparent from the following detailed description taken in conjunction with the annexed drawings, which disclose preferred embodiments of the invention.

BRIEF DESCRIPTION OF THE DRAWINGS

The present invention will be described with respect to the exemplary figures in which like reference numerals refer to like elements and wherein:

5 FIG. 1 shows a generic structure of an item list;

FIG. 2 is an example of two terminal devices that communicate according to an example embodiment of the present invention;

10 FIG. 3 shows a compressed item according to an example embodiment of the present invention;

FIG. 4 shows a compressed item having a compressed item code of "00" according to an example embodiment of the present invention;

15 FIG. 5 shows a compressed item having a compressed item code of "10" according to an example embodiment of the present invention;

FIG. 6 shows a compressed item having a compressed item code of "11" according to an example embodiment of the present invention;

20 FIG. 7 shows a compressed item having a generic encoding scheme according to an example embodiment of the present invention;

FIG. 8 shows a compressed item having an insertion only encoding scheme according to an example embodiment of the present invention;

FIG. 9 shows a structure of a position list according to an example embodiment of the present invention;

25 FIG. 10 shows a compressed item having a removal only encoding scheme according to an example embodiment of the present invention;

FIG. 11 shows a list of position fields and a count field according to an example embodiment of the present invention;

FIG. 12 shows a compressed item having an insertion and removal only encoding scheme according to an example embodiment of the present invention;

5 FIG. 13 shows a compressed item having a content change only encoding scheme according to an example embodiment of the present invention;

FIG. 14 shows a count field and a list of position fields according to an example embodiment of the present invention;

10 FIG. 15 shows a compressed item according to an example embodiment of the present invention;

FIG. 16 shows a compressed item according to an example embodiment of the present invention;

FIG. 17 shows a compressed item according to an example embodiment of the present invention;

15 FIG. 18 shows an example of a compressed item list;

FIG. 19 shows an example of a generic item list compression format;

FIG. 20 shows an example of a compressed item;

FIG. 21 shows an example of a compressed item;

FIG. 22 shows an example of a compressed item; and

20 FIG. 23 shows an example of a compressed item.

DETAILED DESCRIPTION OF PREFERRED EMBODIMENTS

An item list may specify a set of items that is order sensitive. For example, Fig. 1 shows a generic structure of an item list 10 that includes n items numbered 1 to n. Items within the item list 10 may or may not have the same structure. One example of 5 a first case is a Contributing Source (CSRC) list in the Realtime Transport Protocol (RTP) header or an address list in Type 0 IPv6 Routing Header. An example of a second case is an IPv6 extension header.

Fig. 2 shows an example of how information may be communicated between 10 two terminal devices 20 and 30. The first terminal device 20 may include a compressor/decompressor (hereafter called compressor 22) and the second terminal device 30 may also include a decompressor/compressor (hereafter called decompressor 32). Compression and decompression may occur during the communication between the two entities or between any entities that transfer data between each other. For 15 example, header compression may be used between two entities that are connected with a bandwidth limited link (e.g., a radio link). An example of this may be between a mobile node and a base station. The first terminal device 20 and the second terminal device 30 may each include a transmitting/receiving device to transmit/receive signals from one another. The first terminal device 20 and the second terminal device 30 may 20 also both include an encoding/decoding device to perform various encoding/decoding techniques. Operations performed by the devices, as will now be described, may be performed by any one or any combination of the compressor/decompressor, the encoding/decoding device and the transmitting/receiving device.

As will be described below in greater detail, compression of a current item list (i.e., curr_list) may be based on a reference item list (i.e., ref_list) that was previously sent from the terminal device 20 (by the compressor 20) and received at the terminal device 30 (by the decompressor 32). In at least one embodiment, any difference 5 between the current item list and the reference item list may be encoded and sent in a compressed item list. In at least another embodiment, a difference between one item in the current item list and a corresponding item in the reference item list may be encoded and sent in a compressed item in a compressed item list from the terminal device 20 to the terminal device 30.

10 The reference item list (ref_list) may be chosen by any one of various means. One approach may be based on acknowledgment. For example, the compressor 22 may choose the latest item list that is acknowledged by the decompressor 32 as the reference item list. In order to identify the reference item list that will be used for the compression, a reference identifier (i.e., ref_id) may be provided within the compressed 15 item list. A real-time protocol (RTP) sequence number is an example of a reference identifier.

20 Embodiments of the present invention may achieve higher efficiency by encoding and sending the difference between the current item list (curr_list) and the reference item list (ref_list), and by encoding and sending the difference between an item in the current item list and an item in the reference item list. High compression efficiency may be achieved when the size of the current item list is large but only a small portion of the data is changed. The use of a reference item list may provide the

required robustness against errors occurring between the compressor 22 and the decompressor 32.

Embodiments of the present invention may provide three different types of transformation cases. Other embodiments, configurations and numbers of transformation cases are also within the scope of the present invention. A given item in the current item list (curr_list) may be classified as belonging to one of three transformation cases: transformation case A, transformation case B or transformation case C.

In transformation case A, a given item in the current item list (curr_list) is in the reference item list (ref_list), and the contents of these two items are the same. The position of the item in the current item list and the reference item list may or may not be the same. In transformation case B, for the given item in the current item list (curr_list), there is a similarly structured item in the reference item list (ref_list). However, the contents of the item in the current item list and the item in the reference item list are not identical. The position of the item in the current item list and the item in the reference item list may or may not be the same. Finally, in the transformation case C, the given item in the current item list is not in the reference item list.

For the given item in the current item list, the compressor 22 may determine which one of the transformation cases applies. That is, the compressor 22 may determine whether transformation case A applies, whether transformation case B applies, or whether transformation case C applies. Depending on this determination, a

different encoding scheme may be used for the communication to the second terminal device.

A given item in current item list may be compressed using an item in the reference item list as a reference. A compressed item may be referred to as c_item.
5 Fig. 3 shows an example of a compressed item 40 that includes a c_item code (CC) field 42 followed by a c_item data field 44.

For different compressed item codes, contents of the c_item data field 44 may be different. Three different types of compressed item codes and their respective compressed item data may be defined as follows: (1) a c_item code of "0"; (2) a
10 c_item code of "10"; and (3) a c_item code of "11".

A c_item code of "0" may be used for an item classified as belonging to the transformation case A. The structure of the compressed item 40 having a c_item code of "0" may be as shown in Fig. 4. Data within a pos field 46 (i.e., the c_item data) may indicate a position of the item in the reference item list. When the decompressor 32 receives such a compressed item, the decompressor 32 may retrieve the item from the
15 reference item list at the position "pos" and copy the item into the current item list.

The count of "pos" may start at 0. That is, the position of the first item in the list may be 0. Since the pos field 46 in the c_item data field 44 indicates the position of the item in the reference item list, the length of the pos field 46 may depend on the
20 actual number of items in the reference item list. For example, assuming that there are k items in the reference item list, then the number of bits for the pos field 46 may be the ceiling of $(\log_2(k+1))$. More specifically, if there are seven items in the reference

item list, then three bits may be used for the pos field 46. Since the number of items in the reference item list is known to both the compressor 22 and the decompressor 32, both the compressor 22 and the decompressor 32 are aware of the number of bits used in the pos field 46. Accordingly, the length of the pos field 46 does not need to be carried in the compressed list.

5

10

15

A c_item code of "10" may be used for an item classified as belonging to the transformation case B. The structure of the compressed item 40 having the c_item code of "10" may be as shown in Fig. 5. Data within a compressed item field 48 (i.e., the c_item data) may carry a compressed value of the item in the current item list using an item in the reference item list as the reference. The compression technique may be dependent on the item and may be predefined. The position of the item inside the reference item list may be carried in the pos field 46. When the decompressor 32 receives such a compressed item, the decompressor 32 may retrieve the item at the position "pos" in the reference item list and use it as the reference to decompress the compressed item. If the item itself is a list, then the compression scheme may apply to compress the item.

20

A c_item code of "11" may be used for an item classified as belonging to transformation case C. The structure of the compressed item 40 having the c_item code of "11" may be as shown in Fig. 6. Data within an uncompressed item field 50 (i.e., the c_item data) may contain an original value of the item in the current item list. A type-specific data field 52 may contain some additional information used to reconstruct the item list. The presence and the content of the type-specific data field

52 may depend on the item and should be predefined. For example, if the length of each item on the list varies from each other and cannot be obtained from the information inside the item, then a length field may be included within the type-specific data field 52. When the decompressor 32 receives such a compressed item, it may 5 copy the uncompressed item field 50 into the current item list.

List compression will now be described with respect to seven encoding schemes. Other types of list compression, encoding schemes, and number of encoding schemes are also within the scope of the present invention. As will be described, an encoding type field (ET) may be included within the compressed list to identify an 10 encoding scheme used for the list compression. The following different types of encoding schemes will be described: (1) a generic scheme; (2) an insertion only encoding scheme; (3) a removal only encoding scheme; (4) an insertion and removal only encoding scheme; (5) a content change only encoding scheme; (6) an insertion and content change only scheme; and (7) a removal and content change only scheme.

15 The generic encoding scheme will first be described with respect to Figure 7. A generic encoding scheme addresses the situation where the items belong to a mixture of transformation cases. For example, item 1 in a current item list may belong to transformation case B, item 2 may belong to transformation case C, and item 3 may belong to transformation case A. The structure of a compressed item using the generic 20 encoding scheme may be as shown in Fig. 7. The encoding type (ET) field 62 for the generic encoding scheme may be defined as "000". The reference identifier field 64 may contain the reference identifier such as the RTP sequence number. The number of

compressed items in the compressed item list (i.e., c_item 1, ..., c_item n) may be carried in the c_item count field 66. Each compressed item may correspond to one of the items (i.e., item i) in the current item list. Accordingly, the order of the compressed items represents the order of the items in the current item list.

5 An insertion only encoding scheme will now be described with respect to Fig. 8. This insertion only encoding scheme addresses the situation where all the items are classified as belonging to either transformation case C or transformation case A. Fig. 8 shows the structure of the compressed item list.

10 The encoding type (ET) field 62 for the insertion only encoding scheme may be defined as "001". A c_item count field 66 may contain the number of compressed items in the compressed item list (i.e., c_item 1, ..., c_item m). Each compressed item in the compressed item list may correspond to a new item in the compressed item list as compared with the reference item list. An insertion order field 68 may specify the position of the newly added items. Two formats of the insertion order field 68 may be 15 used. For example, an '0' in an aft field 72 may indicate that a bit mask format is used, whereas a "1" in the aft field 72 may indicate that a position list format is used. Selection of the format may depend on the encoding efficiency. If the number of items in the reference item list is large and only a few items are added in the current item list, then the position list format is preferably used; otherwise, the bit mask format may be 20 used. These types of formats are merely example embodiments as other formats are also within the scope of the present invention.

The bit mask format will now be described with respect to the insertion only encoding scheme. In this format, a bit mask may be used to specify a position of the added item. To construct the bit mask and the following compressed item list at the compressor 22, a list of ‘0’ and an empty compressed item list may be generated as the starting point. This may be called a “0” list. The number of ‘0’s in the ‘0’ list may be equal the number of items in the reference item list. The position of each ‘0’ in the ‘0’ list may correspond to the reference item list. That is, the i-th ‘0’ in the ‘0’ list may correspond to the i-th item in the reference item list. Comparing the current item list with the reference item list, if a new item is added between the i-th item and the (i+1)-th item in the reference item list, then a ‘1’ may be inserted between the i-th ‘0’ and (i+1)-th ‘0’ in the original ‘0’ list. The compressed item that carries the new item may be added to the end of the compressed item list. This procedure may be repeated until all the added items have been processed. The length of the bit mask may equal the number of items in the reference item list plus the number of items added into the list.

Since the number of items in the reference item list is known to both the compressor 22 and the decompressor 32, and the number of added items is carried in the c_item count field 66, then the length of the bit mask does not need to be carried in the compressed item list.

When the decompressor 32 receives the bit mask, it may scan the bit mask from left to right. When a ‘0’ is observed, the decompressor 32 may copy the corresponding item in the reference item list into the current item list. On the other

hand, when a ‘1’ is observed, the decompressor 32 may decompress the corresponding compressed item in the current item list and add it into the current item list.

The position list format will now be described. In this format, a list of position fields may be carried in the insertion order field 68. Fig. 9 shows one structure of a position list 80. The i-th field in the position list 80 may correspond to the i-th compressed item in the compressed item list. The value of pos i may indicate the position of the item in the reference item list, before which the added item i should be inserted. The added item i may be obtained from the c_item i. If two or more position fields have the same value (i.e., multiple items are added before a certain item in the reference item list), then a sequence of the added item may depend on the sequence of the respective compressed items with the same position value in the compressed item list.

When the decompressor 32 receives the position list 80, the decompressor 32 may first retrieve all the items in the reference item list. Then, for each compressed item in the compressed item list, the decompressor 32 may obtain the uncompressed value and insert it into the reference item list at the position indicated in the corresponding position field in the position list 80.

A removal only encoding scheme will now be described. The removal only encoding scheme addresses the situations where certain items exist in the reference item list but do not exist in the current item list. Fig. 10 shows a structure of the compressed item list.

The encoding type (ET) field 62 may be defined as "010" for the removal only encoding scheme. A removal order field 82 may contain information regarding which item in the reference item list is not currently in the current item list. Two formats of the removal order field 82 may be used. For example, a '0' in a rft field 84 may indicate that a bit mask format is used, whereas a '1' in the rft field 84 may indicate that a position list format is used. Selection between these formats may depend on the encoding efficiency. If the number of items in the reference item list is small and/or the number of items removed from the reference item list is large, then the bit mask format is preferably used; otherwise the position list format may be used.

10 The bit mask format will now be described with respect to the removal only
encoding scheme. In this format, a removal bit mask may be used. The length of the
removal bit mask may equal the number of items in the reference item list. A '1' in the
i-th bit in the removal bit mask may indicate that the i-th item in the reference item list
is not included in the current item list, whereas a '0' may indicate that it is still present
15 in the current item list. Since the number of items in the reference item list is known to
both the compressor 22 and the decompressor 32, the length of the bit mask does not
need to be sent in the compressed list.

The position list format will now be described with respect to the removal only encoding scheme. In this format as shown in Fig. 11, a list of position fields (i.e., pos 1,...,pos m) and a count field 83 may be included. Each position field may carry the position of an item in the reference item list that no longer exists in the current item list. The count field 83 may carry the number of position fields in the position list.

An insertion and removal only encoding scheme will now be described with respect to Fig. 12. The insertion and removal only encoding scheme accommodates the transformation cases addressed in the insertion only encoding scheme and the removal only encoding scheme. Fig. 12 shows a structure of the compressed item list that is a combination of the structure used in the insertion only encoding scheme and the structure used in the removal only encoding scheme. The encoding type (ET) field 62 may be defined as "011" for the insertion and removal only encoding scheme. The remaining fields relate to their similarly named fields in the insertion only encoding scheme and the removal only encoding scheme.

Unlike the insertion order field in the insertion only encoding scheme, the insertion order field 68 in the insertion and removal only scheme may be based on the items remaining in the reference item list after the removal has been processed. When the decompressor 32 receives such a compressed list, the decompressor 32 may apply the removal before the insertion.

A content change only encoding scheme will now be described with respect to Fig. 13. The content change only encoding scheme addresses the situation where the number of items in the list and the ordering are not changed; however, the content of one or more items is changed. Fig. 13 shows a structure of the compressed item list.

The encoding type (ET) field 62 may be defined as "100" for the content change only encoding scheme. The rft field 84 may specify the format used in a change order field 85. For example, a '0' in the rft field 84 may indicate that a bit mask is used, whereas a '1' in the rft field 84 may indicate that a position list field is used.

The change order field 85 may specify the position of the items whose content is changed. Two formats can be used. In the bit mask format, a change bit mask is included. A '1' in the i -th bit in the change bit mask means that the i -th item in the reference item list is not identical to the i -th item in the current item list, whereas a '0' means that the i -th item in the reference item list is identical to the i -th item in the current item list. Assuming the number of items in the reference item list is k , then the length of the change bit mask equals k . Since k is known to both the compressor 22 and the decompressor 32, it doesn't need to be sent in the compressed list.

In the position list format, a list of position fields as well as a count field is included. Fig. 14 shows the structure of this format. The count field 83 may carry the number of position fields in the position list, which is assumed to be m . A value '0' in the count field 83 may mean that all the items are changed and no position field is included. Assuming that the number of items in the reference item list is k , then the length of the count field 83 may have a ceiling of $(\log_2(k))$. Each position field may carry the position of an item in the reference item list, whose value is not identical with the item at the same position in the current item list. The length of position list may be $m * \text{ceiling}(\log_2(k))$.

Selection between these two formats may depend on the encoding efficiency. If the number of items that have content change is small, then the bit mask format may be more favorable; otherwise, the position list format may be more efficient.

Each compressed item in the compressed item list may correspond to the item whose content is changed when comparing with the item at the same position in the

reference item list. Their positions in the current item list may be represented in the change order field 85. When the position list format is used in the change order field 85 and the count field 83 is '0' then the order of compressed items is the same as the item order in the reference item list. FIG. 15 shows the structure of the compressed item. The C bit field 88 may specify the format of the compressed or uncompressed data field 90. A '0' in the C bit field 88 may indicate that the uncompressed value of the item is sent, whereas a '1' in the C bit field 88 may indicate that the compressed value of the item is carried. The item in the current item list may be compressed using the item at the same position in the reference item list as the reference. The compression technique may be dependent on the item and should be predefined.

An insertion and content change only encoding scheme will now be described. The insertion and content change only encoding scheme addresses the situations where: 1) all the items in the reference item list are also in the current item list, 2) new items are added to the current item list, 3) the relative order of the items that are in both the reference item list and the current item list remains the same, and 4) the content of one or more of these items have been changed. FIG. 16 shows the structure of the compressed item list.

The encoding type (ET) field 62 may be defined as "101" for the insertion and content change only encoding scheme. The remaining fields have been defined in the insertion only encoding scheme and the content change only encoding scheme. The change order field 85 in this scheme is based on the items in the reference item list and the items in the current item list, excluding the newly inserted items. When the

decompressor 32 receives such a compressed list, it applies the content change before the insertion.

A removal and content change only encoding scheme will now be described.

The removal and content change only encoding scheme addresses the situation where:

5 1) some items in the reference item list are not in the current item list, and 2) the content of one or more items that are in both the reference item list and the current item list is changed, but the relative order of these items remains the same. FIG. 17 shows the structure of the compressed item list.

10 The encoding type (ET) field 62 may be defined as "110" for the removal and content change only encoding scheme. The remaining fields have been discussed above with respect to the removal only scheme and the content change only scheme. The change order field 85 in this scheme may be based on the items in the current item list and the items in the reference item list after the removal is processed. When the decompressor 32 receives such a compressed list, it applies the removal before the content change.

15 The following examples illustrate the operation of item list compression under different transformation cases. For these examples, there is not any type-specific data needed for the decompression.

20 A first example will now be described of the insertion and removal only encoding scheme. The items and the order of these items in the current item list are as follows:

current item list: A, B, C, D

reference item list: B, C, X.

By comparing the current item list with the reference item list, it can be determined that A and D are added to the list and X is removed from the list. No change has occurred in the order and the content for B and C. Thus, the format for the insertion and removal only encoding scheme can be used. Fig. 18 shows the compressed item list format for this example.

Since only the compressed items for A and D are included, then the compressed item count in the c_item count field 66 equals two. Assuming both A and D are sent uncompressed, therefore the compressed item for A is "11" plus uncompressed A and the compressed item for D is "11" plus uncompressed D.

Assuming that the bit mask format is used for the removal order, then the rft in the rft field 84 equals '0' and the removal order in the removal order field 82 is "001" where the bits (from left to right) correspond to B, C and X, respectively. The '1' corresponding to X indicates that X is removed. If the position list format is used for the insertion order, then aft in the aft field 72 equals '1', and the insertion order in the insertion order field 68 is "0010". The first two bits "00" indicate that item A is added before the item at position "00" in the reference item list (which is B). The following two bits "10" indicate item D is added before position "10" in the reference item list after the removal is processed (which is after item B).

A second example will now be described of the insertion, removal, change of content and reordering. The items and the order of these items in the current item list and the reference item list are as follows:

current item list: A, C, B', D

5 reference item list: B, C, X.

By comparing the current item list with the reference item list, it can be determined that A and D are added into the list and X is removed from the list. The order of B and C has changed and the content of B has also changed. Fig. 19 shows a generic item list compression format for this example.

10 In this example, the compressed item count in the c_item count field 66 equals four. Additionally, the c_item A may include the fields shown in Fig. 20, and the c_item C may include the fields shown in Fig. 21. In Fig. 21, the "01" may represent the position of C in the reference item list. Further, the c_item B may include the fields shown in Fig. 22. In Fig. 22, the "00" may represent the position of B in the reference item list. The compressed B' may contain the compressed value of B' using B in the reference item list as the reference. The c_item D may include the fields shown in Fig. 15 23.

20 In embodiments described above, it is assumed that a given item in the current item list can be uniquely classified as belonging to one of a plurality of transformation cases. There are other possibilities for doing the classification. One example follows, although others are also within the scope of the present invention.

For a given item (item X) in the current item list, there is no item in the reference item list that has the identical value. However, one item (i.e., item Y) in the reference item list may have the similar value to item X. Therefore, item X can be classified as belonging to either transformation case B or transformation case C. An example of this type of list is CSRC list in RTP headers.

The compressor 22 may decide to use the transformation case in which the encoding scheme will yield the highest compression efficiency. In the above example, we will assume that item X includes L_x bits. If item X is classified as belonging to transformation case A and the compressed item code "11" is used, then the compressed item for item X may include (L_x+2) bits. If item X is classified as belonging to transformation case B and the compressed item code "10" is used (assuming that the length of the position field is L_{pos} and the length of compressed item X when using item Y as the reference is D_{xy}), then the compressed item X may include $(L_{pos}+D_{xy}+2)$ bits. Thus, if $(L_{pos}+D_{xy})$ is larger than L_x , then transformation case B may be used. On the other hand, if $(L_{pos}+D_{xy})$ is not larger than L_x , then transformation case A may be used.

While the invention has been described with reference to specific embodiments, the description of the specific embodiments is illustrative only and is not to be considered as limiting the scope of the invention. That is, various other modifications and changes may occur to those skilled in the art without departing from the spirit and scope of the invention.

